# **Suboptimal Multi-user Receivers Detection Algorithms**

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**Abstract:** Current innovation tries to consistently advance. This movement prompts a ton of examination in any critical region of progress. There is a developing number of end-users in the remote range which has prompted a requirement for improved transmission capacity and BER esteems. At the end of the day, new advancements which would expand the limit of remote frameworks are ending up being an essential purpose of examination in these cutting-edge times. Furthermore, in these modern times, new technologies are proved as research's crucial point that increases the wireless systems' capacities. There have been many multi-user detectors in which the MMSE conducts several linear detector as well as the *n-stage* PIC overcoming the SIC. The assessed detectors were investigated, taking into account even the correlative composition of MAI found in CDMA. In case of high users number as well as because it's basically a matched filters' bank, the limits in multipath and noise occurrence render its use redundant in complicated modern detectors like a traditional linear detector. The MMSE detector are used as a detector's improvement. Therefore, the combination of its collection as one of the linear detectors with other sensors types was investigated. The technology's new field today enables wireless networks to be interpreted as well as explored by many applications. Owing to its wide use within the industry, the software used to simulate this project is MATLAB.

Keywords- Multi User Detection, Single Input- Single Output (SISO) Systems, Successive Interference Cancellation, Parallel Interference Cancellation, Multiple Access Interference.

# **1** Introduction

Today's telecommunications industries' main goal is data, voice as well as their combination's information's reception and transmission; with higher data rates as well as providing considerably low interferences. Wireless networking is one of the fast-growing media largely due to the appeal it offers to end users: mobility. In terms of the development of technology, wireless communication's premature usage as a medium of voice communication must be re-assessed to meet the increasing market for multimedia and text messaging, as used by cell phones. This need created a demand for extremely high data speeds that cannot be provided solely because of the signal interference and finite radio spectrum. Even though wired networks give these preferential rates, connectivity and instantaneity lack the requisite advantages, so research into the achievement of these wireless systems has become a critical research field in today's world.

Excellence is strived by the present world. This feature allows to obtain the most network space, latency and low errors. The last feature of the identification includes multiple people. It is a mixture of methods used to minimize the errors in a contact system's 'receiving' end. The requirement for wider speeds and bandwidths produces the need for recipients that represent minimal errors is of significant importance to MUD. The multi-user scans are a blend of algorithms that easily detects the received multi-user signals. This functionality makes it possible to serially process various MUD combinations to obtain higher error rates and the more visual variations, the more difficult it is. In SISO systems for multi-user detection, the present work offers an overview of the most commonly used techniques. Various SIC, MMSE and ZF detectors combinations were evaluated in order to identify the detector combination. Multi-user receivers can never match the received signals to optimal match [1]. The Optimum Maximum "Likelihood Sequence Estimation Receiver (MLSE)" offers an approach to a perfect match. This receiver has their key limitations in comparison to the system's compute sophistication and the cumulative number of consumers grows exponentially [1]. The optimal CDMA user was obtained by Verdu in 1986 [1]. The implementation of multifunctional identification by Schneider in 1979 was seven years earlier [1] pre-empted. The best recipient is a matched filters' bank to provide user amplitude calculations to a Viterbi decision algorithm for the first-order. Verdu showed mathematically that the optimized receiver has a substantial boost in efficiency relative to the traditional setup, but with the largest number of users in the system, its deployment costs have risen dramatically. This also posed a challenge because the system was greatly complicated. Consequently, detectors are currently planned to be less costly and less robust but now the best detector is used as a benchmark for future solutions. An estimate of the receiver is known to mitigate this significant challenge, leading to the evaluation of "suboptimal" recipients. In Figure 1, you can screen large sizes with multi-user receivers.



Figure 1: Various MUD Configurations

The corresponding advantages and drawbacks are possessed by the various receiver types; thus, it is significant to provide an insight within their theoretical behavior. Two variants occur, linear and non-linear, as seen in Figure 1. In evaluating certain receiver identification algorithms, the architecture obstacles to be addressed are:

- Limitations under Practical Operating Conditions
- Performance versus Complexity
- Linear versus Non-Linear
- Asynchronous versus Synchronous
- Near Far Resistance

## 2. Implementation

## 2.1 Multi-user Detectors for SISO Systems

Signal identification at the receiving end usually utilized in the "single-user" case. When MU transmission advantages arise, that is Figure 2, there is also a requirement for an effective multi-user identification. In the case of existing single-user systems the new 'balanced filter' detector is not appropriate for detecting multimedia signals alone; this is because "Multiple Access Interference (MAI)" is present in the multi-user signals. The deleted signal's BER is disrupted by MAI when utilizing traditional matched filters as the active users' number grows. The MAI is screened off and handled as noise by the matching filters. This MAI also has pieces of the signal, but helpful information is discarded when deciding the exact signal value.



Figure 2: Transmitter of Multi User Detection with CDMA

As referred to above-mentioned Figure 1 MUD receiver classification tree, sub-optimal detectors are primarily of two types. To promote and settle on the option of detectors to use, it is significant to consider the core principles, disadvantages and advantages of devices. For both linear and non-linear situations, the most typical detector configurations were investigated.

#### 2.1.1 Linear Detectors

The linear MU detectors aim at developing decision statistic's refined set with reduced MAI observed by every user, aims at performing a linear operation on the outputs of matched filters, therefore turn out to be near-far resistant. The most commonly used two detectors are mentioned as:

## 2.1.1.1 The De-correlating Detector

It transforms the outputs of matched filters from the initial stage linearly. It decorrelates the user's signals to distinguish the user, e.g. mechanism used to decrease the selfrelation within the signals or cross-correlations in a group of signal and retain another communication facets. This method is done by measuring the cross similarity values of the PN code type as well as storing them in a *KxK* matrix (it is discovered to have complexity of  $K^2$ ). The respective filter outputs' vector is then multiplied by the opposite [2]. Since channel parameters' previous knowledge does not apply, the recipient is insensitive to the near-far effect. The recipient achieves a substantial value in contrast with the traditional paired filter recipient, although the decorrelation mechanism poses a significant drawback to better noise statistics. Because of this downside, the linear detectors studied were ignored.

## 2.1.1.2 The MMSE Detector

The de-correlating detector is identical in its function in comparison to the first stage linear transformation of the matching filter outputs. The detector's purpose is to minimize the average square error among the real data as well as the detected data that is the filter performance. This characteristic resulted in making the MMSE detector more desirable as compared to the detector when noise is amplified. The disadvantage attributable to this characteristic is that the chain parameters must be known [3]. It was observed [4] that a better BER (bit error rates) is possessed by the MMSE than the de-correlator, but at the limit; that is, while the noise level falls to zero, it is similar to the de-correlator's output. A significantly lower almost-far resistance has also been shown [5] [6].

The Least Squares detector is another very useful linear detector which is commonly used. In order to minimize the amount of the squared error, this is similar to the MMSE. The mistake is the subtraction from the initial signal [1] of the observed signal.

#### 2.2 MUD Algorithm for the Linear Detectors

The utilized equations' derivation is as below:

• By utilizing the one-shot demodulation assumption: vector r(i) represents the K users'  $i^{th}$  data symbol, where filter's output matched with  $s_k$  is represented by  $k^{th}$  component in the interval is stated as:

$$r_k(i) = \int_{iT}^{(i+1)T} s_k(t - iT)r(t)dt, \qquad k = 1, 2, \dots K$$
(1)

• The received discrete-time signals are represented in vector form at the *i*<sup>th</sup> symbol instance by assuming every N chip samples as:

$$r(i) = SAb(i) + n(i) \tag{2}$$

• As to the symbol interval's selection, *i* statistical invariance is discovered by discrete-time signal,  $r_k(i)$ ; removal of indices is done deprived of generality loss. Therefore, Equation (2) can be represented in vector form as:

$$r = S\theta + n$$
 where  $\theta = Ab$  (3)

S represents an N by K matrix which holds all K users' signature sequences and  $\theta$  comprises of the sum of the transmitter bits and their corresponding amplitudes. With [8] and (3), the general equation of linear multi-user detection can be described under as

$$\hat{\theta} = Cr = CS\theta + Cn \tag{4}$$

For the  $k^{th}$  user case:

$$\hat{\theta}_{k} = C_{k} s_{k} \theta_{k} + \sum_{j \neq k}^{K} C_{k} s_{k} \theta_{j} + (Cn)_{k}$$
(5)

where, from the received signals for the  $k^{th}$  user estimates  $\hat{\Theta}_k$  are obtained by utilizing the filter,  $C_k$ . Also, within the signal, MAI presence and ambient noise's contribution is shown by the

equation. The correspondence of filter  $C_k$  is observed to linear detector's transfer function. For the three examined detectors that are MMSE, least squares and matched filter are the  $\hat{\Theta}_k$  derivations.

$$\hat{\theta}_{MF} = S^{T}r$$

$$\hat{\theta}_{LS} = (S^{T}S)^{-1}S^{T}r$$

$$\hat{\theta}_{MMSE} = [SA^{2}S^{T} + \sigma 2I]^{-1}SAr$$
(6)

Where, user spreading sequences are represented by S

#### 2.3 Non-Linear Detectors

As in linear detectors, nonlinear multi-user detectors act on the corresponding philtre outputs in a nonlinear way. The most advanced detectors have been tested in recent years. Following is a short summary of their core concepts.

#### 2.3.1 Successive Interference Cancellation (SIC)

This algorithm first determines the strongest user, substitutes him / her from the signal received, and after that detects the most powerful user. You should do so in two ways. It will firstly extract the soft information from the signal received; it contributes to minimal to no error propagation, but it acquires a noise effect accumulating for vulnerable users. Secondly, hard information may be eliminated from processed signals that contribute to little to no noise accumulation due to the potential distribution of errors. Successive interference cancellation may be achieved circularly at the cost of low convergence and therefore higher complexity. The MAI has been diminished and the issue is almost / far greater. The most effective and the most accurate cancellation is the cancellation of the best signal [9]. The SIC algorithm will then most likely be influenced by an error distribution as the most accurate cancellation. Channel estimates at the recipient are also required [9]. The cancellation parallel interference detector, PIC, is another version of this interference detector.

#### **2.3.2 Parallel Interference Cancellation (PIC)**

The PIC detector often includes the removal of other users' interference, close to its predecessor. As its name implies; compared to the SIC series subtraction, the PIC detector cancels the MAI predictions in parallel (i.e. simultaneously) from the output of the matching philter. Its efficiency primarily depends on the estimates of original signal as well as at the source channel estimates are needed. If both consumers are getting the same pressure (e.g. under regulation of power), it works better than SIC [10].

#### 2.3.3 Decision Feedback Equalizer (DFE)

The "DFE (Decision Feedback Equalizer)" is a famous nonlinear equalization technique. The DFE is a very popular one. In the majority of instances, a linear equalizer and a non-linear decision component's combination resulted in DFE. The DFE's aim is to provide both a FIR feed filter and a feedback filter to reduce the interference of the residual intersymbol, ISI. Due to the need for picosecond resolution of decisions in Feedback direction, in

multi-gigabit networks, the DFE is difficult to enforce. DFE conducts linear detectors in terms of efficiency but primarily the difficulty of their implementation and some error propagation problems constitute the big drawback [11]. The particular project consists of combining the MUD techniques' various numbers. Thus, there is a need of every technique's proper dissemination.

# **3** Simulation and Results

# 3.1 Simulation of Linear Detectors

The technology's new field today enables wireless networks to be interpreted as well as explored by many applications. Owing to its wide use within the industry, the software used to simulate this project is "MATLAB." This Programme is user-friendly and is intended to provide engineers and scientists with the best approximation possible to model every day activities. The project aim is very precise but execution is very complex since multiple communication mechanisms are interconnected. Following are the major phases used in this project:

- For single carrier CDMA, designing as well as simulating linear multi-user detectors
- Combining a PIC receiver with the selected linear detector
- By using a MIMO architecture, it is extended
- Through Sphere Decoding Algorithm's incorporation total performance is improved

The following simulations sum up the initial process of the experiment. The contrast included two large linear detectors of industries, the MMSE and Least Squares detector, which were the traditional mixed filters detector in combination. MMSE and PIC have integrated the optimal alternative and measured their success.

This was obtained by means of MATLAB to compare the following three sensors; the MMSE detector, least squares detector and conventional matched filter.

- BER vs. number of Users, as represented in Figure 3.
- BER vs. S/N Ratio, with distinct users' number, as represented in Figure 4 & 5.



Figure 3: Bit Error Rate Versus Number of Users



Figure 4: Bit Error Rate Versus Signal-to-Noise Ratio with user count 5



Figure 5: Bit Error Rate Versus Signal-to-Noise Ratio with user count 10

The Fig.3, 4 as well as Fig.5 results explicitly illustrate the benefits that the MMSE detector provides in contrast to the traditional mixed filter detectors as well as lowest square. These statistics indicate that MMSE offers a better SNR for a growing number of users as well as provides better BERs. The statistics illustrate the need to identify multiple users, as the traditional mixed filter deteriorate with active users' growing number. In Fig.5, the MF calculation indicates a high rate of roll-off relative to Figure 4, which is historically the MF calculation.

## 3.2 Simulation of Non-Linear Receiver Combinations

The early simulations have shown that when compared with their previously described predecessors, MMSE provides substantial enhancements. The ever-growing need for higher data speeds, however, demands much greater BER upgrades. The combination of the MMSE and PIC algorithms, which have also been researched in previous literature, [4], is envisaged for this reason. An N-stage System has been studied for a receptor with this configuration. The BER values increase with rising PIC measures can be seen very clearly in Figure 6. However, it is worth noting that with phase numbers that lead to tradeoffs at times of system design, the

complexity of the PIC system increases. The MMSE stage addition to the PIC algorithm also indicates in figure 6 that the BER value is higher. However, compared with the standalone PIC simulations, this implementation enhanced simulation performance.



Figure 6: Bit Error Rate for n-stage PIC Detector

It is significantly noted that as  $\sigma \rightarrow 0$  that means wireless channel which is noiseless; simply a simple PIC algorithm is approximated by the MMSE/PIC because of the reason that a matched filter is approximated by the MMSE counterpart.

## 4. Conclusion

There have been many multi-user detectors in which the MMSE conducts several linear detector as well as the *n-stage* PIC overcoming the SIC. The assessed detectors were investigated, taking into account even the correlative composition of MAI found in CDMA. In case of high users number as well as because it's basically a matched filters' bank, the limits in multipath and noise occurrence render its use redundant in complicated modern detectors like a traditional linear detector. The MMSE detector are used as a detector's improvement.

PIC and SIC algorithms also outweigh their MMSE and MF counterparts. It is also shown. The MMSE / PIC detector's principal appeal is how to boost the signal receiving by interfering with the incident device noise.

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